

**Reading:** Friedland 11 (Frequency-Severity Methods)  
**Model:** 2017.Fall #20  
**Problem Type:** Reserving Methods - FS (Exposures & Trends 020)

F-11 (020) FS (Problem 1)

**Find** Calculate the **ultimate** for AY 2025 using a frequency-severity method.

*\* Note the actual exam problem asks for the BF ultimate where the result of the frequency-severity method is used as the 'a-priori' initial estimate in the BF formula*

**Given**

AY	payroll (000s)	rptd loss (000s)	indicated	
			ultimate counts	selected severity
2022	68,000	3,470	1,090	3,400
2023	71,500	2,151	1,000	3,600
2024	75,200	1,377	1,130	?
2025	79,000	1,033	?	?

annual trend for exposures (payroll inflation rate)	5%
annual trend for counts	1%
annual trend for severity	7%

**Step 1** calculate frequency **trended to 2025**:  $(\text{trended counts}) / (\text{trended exposures})$

AY	counts	count trd fctr	payroll	payroll trd fctr	trended frequency
2022	1,090	1.01^3	68,000	1.05^3	1.427%
2023	1,000	1.01^2	71,500	1.05^2	1.294%
2024	1,130	1.01^1	75,200	1.05^1	1.445%
2025					<b>1.436%</b>

*Unless there is an obvious outlier, you are usually safe selecting the average because there are only 3 data points.*

*<-- average excluding AY 2023*

**Step 2** calculate severity **trended to 2025**:  $\text{apply severity trend to given selected severities}$

AY	selected severity	severity trd fctr	trended severity
2022	3,400	1.07^3	4,165
2023	3,600	1.07^2	4,122
2024	n/a	n/a	n/a
2025			4,143

*With only 2 data points, you really have no choice but to select the average*

*<-- default selection = all period average*

**Step 3** calculate the ultimate for **AY 2025** (in 000s)

$$\begin{aligned}
 \text{ultimate} &= \text{exposure} \times \text{frequency} \times \text{severity} / 1,000 \\
 &= 79,000 \times 1.436\% \times 4,143 / 1,000 \\
 &= \mathbf{4,701} \quad \text{<-- final answer}
 \end{aligned}$$

**Reading:** Friedland 11 (Frequency-Severity Methods)  
**Model:** 2017.Fall #20  
**Problem Type:** Reserving Methods - FS (Exposures & Trends 020)

F-11 (020) FS (Problem 2)

**Find** Calculate the **ultimate** for AY 2025 using a frequency-severity method.

*\* Note the actual exam problem asks for the BF ultimate where the result of the frequency-severity method is used as the 'a-priori' initial estimate in the BF formula*

**Given**

AY	payroll (000s)	rptd loss (000s)	indicated	
			ultimate counts	selected severity
2022	24,000	1,320	340	1,400
2023	24,700	937	420	1,100
2024	25,500	562	410	?
2025	26,200	343	?	?

annual trend for exposures (payroll inflation rate)	3%
annual trend for counts	1%
annual trend for severity	10%

**Step 1** calculate frequency **trended to 2025**:  $(\text{trended counts}) / (\text{trended exposures})$

AY	counts	count trd fctr	payroll	payroll trd fctr	trended frequency
2022	340	1.01^3	24,000	1.03^3	1.336%
2023	420	1.01^2	24,700	1.03^2	1.635%
2024	410	1.01^1	25,500	1.03^1	1.577%
2025					<b>1.606%</b>

*Unless there is an obvious outlier, you are usually safe selecting the average because there are only 3 data points.*

*<-- average excluding AY 2022*

**Step 2** calculate severity **trended to 2025**:  $\text{apply severity trend to given selected severities}$

AY	selected severity	severity trd fctr	trended severity
2022	1,400	1.1^3	1,863
2023	1,100	1.1^2	1,331
2024	n/a	n/a	n/a
2025			1,597

*With only 2 data points, you really have no choice but to select the average*

*<-- default selection = all period average*

**Step 3** calculate the ultimate for **AY 2025** (in 000s)

$$\begin{aligned}
 \text{ultimate} &= \text{exposure} \times \text{frequency} \times \text{severity} / 1,000 \\
 &= 26,200 \times 1.606\% \times 1,597 / 1,000 \\
 &= \mathbf{672} \quad \text{<-- final answer}
 \end{aligned}$$