(Fr16.ALAE) 03a-Question

Reading: Friedland 16 (ALAE)
Model: 2019.Spring #24

**Problem Type:** Additive or Multiplicative approach for ALAE

| Problem | Use the  | multiplicative | approach to estimate the | ultimate | ALAE                                    | for AY | 2019 |
|---------|----------|----------------|--------------------------|----------|---|--------|------|
|         | OSC tile | manapheative   | approach to estimate the | artimate | , ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, | 101711 | 2010 |

cumulative paid claims: cumulative paid ALAE:

| AY   | 12    | 24     | 36     | 48     | AY   | 12  | 24  | 36  | 48  |
|------|-------|--------|--------|--------|------|-----|-----|-----|-----|
| 2016 | 4,400 | 12,700 | 19,800 | 22,000 | 2016 | 123 | 506 | 818 | 882 |
| 2017 | 5,000 | 14,600 | 20,800 |        | 2017 | 100 | 391 | 657 |     |
| 2018 | 3,600 | 10,900 |        |        | 2018 | 104 | 467 |     |     |
| 2019 | 4,000 |        |        |        | 2019 | 120 |     |     |     |

selected ultimate claims by AY

| AY   | ult clms | <=== | sometimes you are not given the ultimate claims                     |
|------|----------|------|---|
| 2016 | 22,000   |      | - you would then have to calculate them using an appropriate method |
| 2017 | 22,428   |      | - see 2016.Spring #23   |
| 2018 | 17,023   |      |   |
| 2019 | 19,128   |      |   |

Step 1: Ratio of cumulative paid ALAE to cumulative paid claims:

| AY   | 12    | 24    | 36    | 48    |
|------|-------|-------|-------|-------|
| 2016 | 2.80% | 3.98% | 4.13% | 4.01% |
| 2017 | 2.00% | 2.68% | 3.16% |       |
| 2018 | 2.89% | 4.28% |       |       |
| 2019 | 3.00% |       |       |       |

## Step 2: Development triangle (either additive or multiplicative as appropriate):

| AY        | 12-24  | 24-36  | 36-48  | 48-    |      |   |
|-----------|--------|--------|--------|--------|------|---|
| 2016      | 1.4214 | 1.0377 | 0.9709 |        | <=== | MULTIPLICATIVE development                          |
| 2017      | 1.3400 | 1.1791 |        |        |      |   |
| 2018      | 1.4810 |        |        |        |      |   |
| 2019      |        |        |        |        |      |   |
| selected  | 1.4141 | 1.1084 | 0.9709 | 1.0000 | <=== | tail = 0.0 if additive OR 1.0 if multiplicative     |
| cum       | 1.5217 | 1.0761 | 0.9709 | 1.0000 | <=== | MULTIPLICATIVE: selected x (previous cum)           |
| Ult Ratio | 4.57%  | 4.61%  | 3.07%  | 4.01%  | <=== | MULTIPLICATIVE: cum x (latest diagonal from Step 1) |
|           | •      |        |        |        | _    |   |
| AY        | 2019   | 2018   | 2017   | 2016   | <=== | given information                                   |
| ult clms  | 19,128 | 17,023 | 22,428 | 22,000 |      | (provided here for convenience)                     |
| pd ALAE   | 120    | 467    | 657    | 882    |      |   |

Step 3: Ultimate ALAE = (Ultimate Ratio) x (Ultimate Claims)
Unpad ALAE = (Ultimate ALAE) - (Paid ALAE)

| AY   | Ult ALAE | UnPd ALAE |
|------|----------|-----------|
| 2016 | 882.2    | 0.2       |
| 2017 | 688.5    | 31.5      |
| 2018 | 784.8    | 317.8     |
| 2019 | 874.1    | 754.1     |
|      | 3,229.6  | 1,103.6   |
|      |          |           |

Step 4: <u>ultimate</u> ALAE for AY <u>2019</u> = 874.1 <=== final answe

(Fr16.ALAE) 04a-Question

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**Problem Type:** Additive or Multiplicative approach for ALAE

 Problem
 Use the
 multiplicative
 approach to estimate the
 unpaid
 ALAE
 for AY
 2020

cumulative paid claims:

cumulative paid ALAE:

| AY   | 12    | 24     | 36     | 48     | AY   | 12  | 24  | 36  | 48  |
|------|-------|--------|--------|--------|------|-----|-----|-----|-----|
| 2018 | 3,500 | 9,600  | 14,700 | 16,300 | 2018 | 91  | 397 | 603 | 657 |
| 2019 | 3,400 | 9,600  | 14,800 |        | 2019 | 71  | 322 | 526 |     |
| 2020 | 3,800 | 11,200 |        |        | 2020 | 103 | 463 |     |     |
| 2021 | 3,800 |        |        |        | 2021 | 114 |     |     |     |

selected ultimate claims by AY

| AY   | ult clms | <=== |
|------|----------|------|
| 2018 | 16,300   |      |
| 2019 | 16,650   |      |
| 2020 | 18,860   |      |
| 2021 | 17,825   |      |

sometimes you are not given the ultimate claims

- you would then have to calculate them using an appropriate method
- see 2016.Spring #23

Step 1: Ratio of cumulative paid ALAE to cumulative paid claims:

| AY   | 12    | 24    | 36    | 48    |
|------|-------|-------|-------|-------|
| 2018 | 2.60% | 4.14% | 4.10% | 4.03% |
| 2019 | 2.09% | 3.35% | 3.55% |       |
| 2020 | 2.71% | 4.13% |       |       |
| 2021 | 3.00% |       |       |       |

## Step 2: Development triangle (either additive or multiplicative as appropriate):

| AY        | 12-24  | 24-36  | 36-48  | 48-    |      |   |
|-----------|--------|--------|--------|--------|------|---|
| 2018      | 1.5923 | 0.9903 | 0.9829 |        | <=== | MULTIPLICATIVE development                          |
| 2019      | 1.6029 | 1.0597 |        |        |      |   |
| 2020      | 1.5240 |        |        |        |      |   |
| 2021      |        |        |        |        | _    |   |
| selected  | 1.5731 | 1.0250 | 0.9829 | 1.0000 | <=== | tail = 0.0 if additive OR 1.0 if multiplicative     |
| cum       | 1.5849 | 1.0075 | 0.9829 | 1.0000 | <=== | MULTIPLICATIVE: selected x (previous cum)           |
| Ult Ratio | 4.75%  | 4.16%  | 3.49%  | 4.03%  | <=== | MULTIPLICATIVE: cum x (latest diagonal from Step 1) |
|           |        |        |        |        |      |   |
| AY        | 2021   | 2020   | 2019   | 2018   | <=== | given information                                   |
| ult clms  | 17,825 | 18,860 | 16,650 | 16,300 |      | (provided here for convenience)                     |
| pd ALAE   | 114    | 463    | 526    | 657    | ]    |   |

Step 3: Ultimate ALAE = (Ultimate Ratio) x (Ultimate Claims)
Unpad ALAE = (Ultimate ALAE) - (Paid ALAE)

| Ult ALAE | UnPd ALAE                        |
|----------|----------------------------------|
| 656.9    | (0.1)                            |
| 581.1    | 55.1                             |
| 784.6    | 321.6                            |
| 846.7    | 732.7                            |
| 2,869.2  | 1,109.2                          |
|          | 656.9<br>581.1<br>784.6<br>846.7 |

Step 4: <u>unpaid</u> ALAE for AY <u>2020</u> = 321.6 <=== final answe

(Fr16.ALAE) 05a-Question

Reading: Friedland 16 (ALAE)
Model: 2019.Spring #24

**Problem Type:** Additive or Multiplicative approach for ALAE

 Problem
 Use the
 additive
 approach to estimate the
 ultimate
 ALAE
 for AY
 2019

cumulative paid claims: cumulative paid ALAE:

| AY   | 12    | 24     | 36     | 48     | AY   | 12  | 24  | 36  | 48  |
|------|-------|--------|--------|--------|------|-----|-----|-----|-----|
| 2017 | 4,300 | 13,900 | 20,900 | 22,800 | 2017 | 116 | 507 | 803 | 866 |
| 2018 | 4,500 | 13,900 | 21,500 |        | 2018 | 99  | 428 | 719 |     |
| 2019 | 3,700 | 11,800 |        |        | 2019 | 89  | 396 |     |     |
| 2020 | 4,400 |        |        |        | 2020 | 110 |     |     |     |

selected ultimate claims by AY

|   | ΑY  | ult clms | <=== | sometimes you are not given the ultimate claims                     |
|---|-----|----------|------|---|
| 2 | 017 | 22,800   |      | - you would then have to calculate them using an appropriate method |
| 2 | 018 | 23,129   |      | - see 2016.Spring #23   |
| 2 | 019 | 19,137   |      |   |
| 2 | 020 | 21,398   |      |   |

Step 1: Ratio of cumulative paid ALAE to cumulative paid claims:

| AY   | 12    | 24    | 36    | 48    |
|------|-------|-------|-------|-------|
| 2017 | 2.70% | 3.65% | 3.84% | 3.80% |
| 2018 | 2.20% | 3.08% | 3.34% |       |
| 2019 | 2.41% | 3.36% |       |       |
| 2020 | 2.50% |       |       |       |

Step 2: Development triangle (either additive or multiplicative as appropriate):

| AY        | 12-24  | 24-36  | 36-48   | 48-    | _    |   |
|-----------|--------|--------|---------|--------|------|---|
| 2017      | 0.0095 | 0.0019 | -0.0004 |        | <=== | ADDITIVE development                            |
| 2018      | 0.0088 | 0.0026 |         |        |      |   |
| 2019      | 0.0095 |        |         |        |      |   |
| 2020      |        |        |         |        | _    |   |
| selected  | 0.0093 | 0.0023 | -0.0004 | 0.0000 | <=== | tail = 0.0 if additive OR 1.0 if multiplicative |
| cum       | 0.0112 | 0.0019 | -0.0004 | 0.0000 | <=== | ADDITIVE: selected + (previous cum)             |
| Ult Ratio | 3.62%  | 3.55%  | 3.30%   | 3.80%  | <=== | ADDITIVE: cum + (latest diagonal from Step 1)   |
|           |        |        |         |        | _    |   |
| AY        | 2020   | 2019   | 2018    | 2017   | <=== | given information                               |
| ult clms  | 21,398 | 19,137 | 23,129  | 22,800 |      | (provided here for convenience)                 |
| pd ALAE   | 110    | 396    | 719     | 866    |      |   |

Step 3: Ultimate ALAE = (Ultimate Ratio) x (Ultimate Claims)
Unpad ALAE = (Ultimate ALAE) - (Paid ALAE)

| AY   | Ult ALAE | UnPd ALAE |
|------|----------|-----------|
| 2017 | 866.4    | 0.4       |
| 2018 | 763.3    | 44.3      |
| 2019 | 679.4    | 283.4     |
| 2020 | 774.6    | 664.6     |
|      | 3,083.6  | 992.6     |
|      |          |           |

Step 4: <u>ultimate</u> ALAE for AY <u>2019</u> = 679.4 <=== final answe

(Fr16.ALAE) 06a-Question

Reading: Friedland 16 (ALAE)
Model: 2019.Spring #24

**Problem Type:** Additive or Multiplicative approach for ALAE

 Problem
 Use the
 additive
 approach to estimate the
 unpaid
 ALAE
 for AY
 2020

cumulative paid claims: cumulative paid ALAE:

| AY   | 12    | 24     | 36     | 48     | AY   | 12  | 24  | 36  | 48  |
|------|-------|--------|--------|--------|------|-----|-----|-----|-----|
| 2017 | 5,100 | 13,900 | 20,600 | 22,200 | 2017 | 107 | 458 | 747 | 838 |
| 2018 | 5,100 | 16,100 | 23,700 |        | 2018 | 128 | 554 | 878 |     |
| 2019 | 4,800 | 13,700 |        |        | 2019 | 110 | 462 |     |     |
| 2020 | 5,800 |        |        |        | 2020 | 133 |     |     |     |

selected ultimate claims by AY

| AY       | ult clms | <=== | sometimes you are not given the ultimate claims                     |
|----------|----------|------|---|
| <br>2017 | 22,200   |      | - you would then have to calculate them using an appropriate method |
| 2018     | 25,855   |      | - see 2016.Spring #23   |
| 2019     | 22,196   |      |   |
| 2020     | 27,008   |      |   |

Step 1: Ratio of cumulative paid ALAE to cumulative paid claims:

| AY   | 12    | 24    | 36    | 48    |
|------|-------|-------|-------|-------|
| 2017 | 2.10% | 3.29% | 3.63% | 3.77% |
| 2018 | 2.51% | 3.44% | 3.70% |       |
| 2019 | 2.29% | 3.37% |       |       |
| 2020 | 2.29% |       |       |       |

Step 2: Development triangle (either additive or multiplicative as appropriate):

| AY        | 12-24  | 24-36  | 36-48  | 48-    |      |   |
|-----------|--------|--------|--------|--------|------|---|
| 2017      | 0.0119 | 0.0034 | 0.0014 |        | <=== | ADDITIVE development                            |
| 2018      | 0.0093 | 0.0026 |        |        |      |   |
| 2019      | 0.0108 |        |        |        |      |   |
| 2020      |        |        |        |        | _    |   |
| selected  | 0.0107 | 0.0030 | 0.0014 | 0.0000 | <=== | tail = 0.0 if additive OR 1.0 if multiplicative |
| cum       | 0.0151 | 0.0044 | 0.0014 | 0.0000 | <=== | ADDITIVE: selected + (previous cum)             |
| Ult Ratio | 3.80%  | 3.81%  | 3.84%  | 3.77%  | <=== | ADDITIVE: cum + (latest diagonal from Step 1)   |
|           |        |        |        |        | _    |   |
| AY        | 2020   | 2019   | 2018   | 2017   | <=== | given information                               |
| ult clms  | 27,008 | 22,196 | 25,855 | 22,200 |      | (provided here for convenience)                 |
| pd ALAE   | 133    | 462    | 878    | 838    |      |   |

Step 3: Ultimate ALAE
Unpad ALAE

= (Ultimate Ratio)

(Ultimate Claims)

= (Ultimate ALAE)

(Paid ALAE)

| Ult ALAE | UnPd ALAE                          |
|----------|------------------------------------|
| 836.9    | (1.1)                              |
| 992.8    | 114.8                              |
| 845.7    | 383.7                              |
| 1,026.3  | 893.3                              |
| 3,701.7  | 1,390.7                            |
|          | 836.9<br>992.8<br>845.7<br>1,026.3 |

Step 4: <u>unpaid</u> ALAE for AY <u>2020</u> = 893.3 <=== final answer