

Reading: Werner 05: Premium
Model: Pricing Components
Problem Type: Premium Development

W-05 (030) Premium Devlpt (Problem 1)

Find Calculate the PY premium development factor year-end: 2026

Given WC carrier writes 1 annual policy per month in 2025 (assume first day of month)

Estimated premium at policy inception: 500
Months after policy expiration until first audit: 3
Historical upward premium development at audit 10%

Step 1 calculate number of policies with audit complete by year-end

2026

$$\begin{aligned}
 n &= 12 - (\text{months after policy expiration until first audit}) \\
 &= 12 - 3 \\
 &= 9
 \end{aligned}$$

Step 2a calculate PY written premium as of year-end

2026

$$\begin{aligned}
 \text{Current PY WP} &= n \times (\text{est. premium}) \times (\text{historical upward development}) \\
 &+ (12 - n) \times (\text{est. premium}) \\
 &= 9 \times 500 \times 1.10 \\
 &+ 3 \times 500 \\
 &= 6,450
 \end{aligned}$$

Step 2b calculate final PY written premium at year-end

2027

(all policy audits are now complete)

$$\begin{aligned}
 \text{Final PY WP} &= 12 \times (\text{est. premium}) \times (\text{historical upward development}) \\
 &= 12 \times 500 \times 1.10 \\
 &= 6,600
 \end{aligned}$$

Step 3 calculate premium development factor

$$\begin{aligned}
 \text{PDF} &= \frac{\text{step 2b}}{\text{step 2a}} \\
 &= \frac{6,600}{6,450} \\
 &= 1.0233 \\
 &\quad \text{(final answer)}
 \end{aligned}$$

Step 1 calculate number of policies with audit complete by year-end

2026

$$\begin{aligned}
 n &= 12 - (\text{months after policy expiration until first audit}) \\
 &= 12 - 3 \\
 &= 9
 \end{aligned}$$

Step 2a calculate PY written premium as of year-end

2026

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W-05 (030) Premium Devlpt (Problem 2)

Find Calculate the PY premium development factor year-end: 2026

Given WC carrier writes 1 annual policy per month in 2025 (assume first day of month)

Estimated premium at policy inception: 750
Months after policy expiration until first audit: 9
Historical upward premium development at audit 15%

Step 1 calculate number of policies with audit complete by year-end

2026

$$\begin{aligned}
 n &= 12 - (\text{months after policy expiration until first audit}) \\
 &= 12 - 9 \\
 &= 3
 \end{aligned}$$

Step 2a calculate PY written premium as of year-end

2026

$$\begin{aligned}
 \text{Current PY WP} &= n \times (\text{est. premium}) \times (\text{historical upward development}) \\
 &+ (12 - n) \times (\text{est. premium}) \\
 &= 3 \times 750 \times 1.15 \\
 &+ 9 \times 750 \\
 &= 9,338
 \end{aligned}$$

Step 2b calculate final PY written premium at year-end

2027

(all policy audits are now complete)

$$\begin{aligned}
 \text{Final PY WP} &= 12 \times (\text{est. premium}) \times (\text{historical upward development}) \\
 &= 12 \times 750 \times 1.15 \\
 &= 10,350
 \end{aligned}$$

Step 3 calculate premium development factor

$$\begin{aligned}
 \text{PDF} &= \frac{\text{step 2b}}{\text{step 2a}} \\
 &= \frac{10,350}{9,338} \\
 &= 1.1084 \\
 &\quad \text{(final answer)}
 \end{aligned}$$