

Reading: Werner 12: Credibility
Model: Text Example
Problem Type: Increased Limits Analysis

ILA (210) - (Problem 1)

Find Find the complement of credibility in indicated layer using Increased Limits Analysis.

Given layer: 250,000 to 1,000,000

losses on policies capped at: 250,000 is 500,000

increased limits factors:

limit	ILF
50,000	1.00
100,000	1.50
250,000	1.75
500,000	2.50
1,000,000	3.50
2,000,000	4.25

Step 1 just apply the formula to find the complement of credibility C

A	=	250,000	<====	Attachment point
A + L	=	1,000,000	<====	Attachment point + Limit of insurer's liability
ILF(A)	=	1.75	<====	lookup on ILF table
ILF(A+L)	=	3.50	<====	lookup on ILF table

now just apply the formula

$$\begin{aligned}
 C &= \text{cap} / \text{ILF(A)} \times (\text{ILF(A+L)} - \text{ILF(A)}) \\
 &= 500,000 / 1.75 \times (3.50 - 1.75) \\
 &= 500,000
 \end{aligned}$$

Reading: Werner 12: Credibility
Model: Text Example
Problem Type: Increased Limits Analysis

ILA (210) - (Problem 2)

Find Find the complement of credibility in indicated layer using Increased Limits Analysis.

Given layer: 100,000 to 500,000

losses on policies capped at: 100,000 is 300,000

increased limits factors:

limit	ILF
50,000	1.00
100,000	1.75
250,000	2.50
500,000	3.00
1,000,000	3.50
2,000,000	4.00

Step 1 just apply the formula to find the complement of credibility C

A	=	100,000	<====	Attachment point
A + L	=	500,000	<====	Attachment point + Limit of insurer's liability
ILF(A)	=	1.75	<====	lookup on ILF table
ILF(A+L)	=	3.00	<====	lookup on ILF table

now just apply the formula

$$\begin{aligned}
 C &= \text{cap} / \text{ILF(A)} \times (\text{ILF(A+L)} - \text{ILF(A)}) \\
 &= 300,000 / 1.75 \times (3.00 - 1.75) \\
 &= 214,286
 \end{aligned}$$

Reading: Werner 12: Credibility
Model: Text Example
Problem Type: Lower Limits Analysis - Complements for Excess Ratemating

LLA (220) - (Problem 1)

Find Find the complement of credibility in indicated layer using Lower Limits Analysis.

Given layer: 250,000 to 1,000,000

losses on policies capped at: 50,000 is 100,000

increased limits factors:

limit	ILF
50,000	1.20
100,000	1.70
250,000	1.95
500,000	2.20
1,000,000	3.20
2,000,000	3.95

Step 1 just apply the formula to find the complement of credibility C

d	=	50,000	<====	lower limit
A	=	250,000	<====	Attachment point
A + L	=	1,000,000	<====	Attachment point + Limit of insurer's liability
ILF(d)	=	1.20	<====	lookup on ILF table
ILF(A)	=	1.95	<====	lookup on ILF table
ILF(A+L)	=	3.20	<====	lookup on ILF table

now just apply the formula

$$\begin{aligned}
 C &= \text{cap} / \text{ILF(d)} \times (\text{ILF(A+L)} - \text{ILF(A)}) \\
 &= 100,000 / 1.20 \times (3.20 - 1.95) \\
 &= 104,167
 \end{aligned}$$

Reading: Werner 12: Credibility
Model: Text Example
Problem Type: Lower Limits Analysis - Complements for Excess Ratemating

LLA (220) - (Problem 2)

Find Find the complement of credibility in indicated layer using Lower Limits Analysis.

Given layer: 100,000 to 2,000,000

losses on policies capped at: 50,000 is 150,000

increased limits factors:

limit	ILF
50,000	1.10
100,000	1.35
250,000	1.85
500,000	2.10
1,000,000	2.85
2,000,000	3.60

Step 1 just apply the formula to find the complement of credibility C

d	=	50,000	<====	lower limit
A	=	100,000	<====	Attachment point
A + L	=	2,000,000	<====	Attachment point + Limit of insurer's liability
ILF(d)	=	1.10	<====	lookup on ILF table
ILF(A)	=	1.35	<====	lookup on ILF table
ILF(A+L)	=	3.60	<====	lookup on ILF table

now just apply the formula

$$\begin{aligned}
 C &= \text{cap} / \text{ILF(d)} \times (\text{ILF(A+L)} - \text{ILF(A)}) \\
 &= 150,000 / 1.10 \times (3.60 - 1.35) \\
 &= 306,818
 \end{aligned}$$

Reading: Werner 12: Credibility
Model: Text Example
Problem Type: Lower Limits Analysis - Complements for Excess Ratemating

LA (230) - (Problem 1)

Find Find the complement of credibility in indicated layer using **Limits Analysis**.

Given layer: 250,000 to 500,000

estimated all limits LR: 68%

increased limits factors:

limit (d)	premium	ILF
50,000	1,000,000	1.00
100,000	700,000	1.50
250,000	600,000	2.25
500,000	300,000	3.00
1,000,000	300,000	4.00

Step 1 let's get everything organized so that step 2 is easy

d	=	cycles over all values greater than or equal to A		
A	=	250,000	<====	Attachment point
A + L	=	500,000	<====	Attachment point + Limit of insurer's liability
ILF(d)	=	depends on which row we're on in the table		
ILF(A)	=	2.25	<====	lookup on ILF table
ILF(A+L)	=	3.00	<====	lookup on ILF table

Step 2 set up the table to do the calculations

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
d	A + L	min(d,A+L)	expected total losses	ILF for min(d,A+L)	ILF(A)	ILF(d)	% loss in layer	expected loss in layer
50,000	500,000	50,000	680,000	1.00	2.25	1.00	0.00%	0
100,000	500,000	100,000	476,000	1.50	2.25	1.50	0.00%	0
250,000	500,000	250,000	408,000	2.25	2.25	2.25	0.00%	0
500,000	500,000	500,000	204,000	3.00	2.25	3.00	25.00%	51,000
1,000,000	500,000	500,000	204,000	3.00	2.25	4.00	18.75%	38,250
								89,250

(4) = (premium for each limit d) x (estimated all limits LR)

(8) = MAX [0 , [(5)-(6)] / (7)]

(9) = (4) x (8)

(final answer)

Note: You can probably do this calculation with fewer columns in the table. Alice wrote out all the intermediate steps because it's just too easy to mess this up. Slowly and correctly beats rapidly and stupidly. :-)

Reading: Werner 12: Credibility
Model: Text Example
Problem Type: Lower Limits Analysis - Complements for Excess Ratemating

LA (230) - (Problem 2)

Find Find the complement of credibility in indicated layer using **Limits Analysis**.

Given layer: 50,000 to 100,000

estimated all limits LR: 79%

increased limits factors:

limit (d)	premium	ILF
50,000	1,400,000	1.00
100,000	600,000	1.50
250,000	500,000	2.00
500,000	400,000	2.50
1,000,000	300,000	3.25

Step 1 let's get everything organized so that step 2 is easy

d = cycles over all values greater than or equal to A
 A = 50,000 <==== Attachment point
 $A + L$ = 100,000 <==== Attachment point + Limit of insurer's liability

 $ILF(d)$ = depends on which row we're on in the table
 $ILF(A)$ = 1.00 <==== lookup on ILF table
 $ILF(A+L)$ = 1.50 <==== lookup on ILF table

Step 2 set up the table to do the calculations

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
d	$A + L$	$\min(d, A+L)$	expected total losses	ILF for $\min(d, A+L)$	$ILF(A)$	$ILF(d)$	% loss in layer	expected loss in layer
50,000	100,000	50,000	1,106,000	1.00	1.00	1.00	0.00%	0
100,000	100,000	100,000	474,000	1.50	1.00	1.50	33.33%	158,000
250,000	100,000	100,000	395,000	1.50	1.00	2.00	25.00%	98,750
500,000	100,000	100,000	316,000	1.50	1.00	2.50	20.00%	63,200
1,000,000	100,000	100,000	237,000	1.50	1.00	3.25	15.38%	36,462
								356,412

(4) = (premium for each limit d) x (estimated all limits LR)

(8) = $\text{MAX} [0, [(5)-(6)] / (7)]$

(9) = (4) x (8)

(final answer)

Note: You can probably do this calculation with fewer columns in the table. Alice wrote out all the intermediate steps because it's just too easy to mess this up. Slowly and correctly beats rapidly and stupidly. :-)