

Reading: Werner 14: Implementation
Model: Text Example
Problem Type: Limiting Premium Effect of a Single Variable (Non-Base Level)

W-14 (080) - (Problem 1)

Find Calculate the relativities that satisfy the given requirements.

overall rate change	5%
maximm premium increase for any level of the rating variable	15%

Given **Rating variable information prior to capping**

level	premium	current	indicated
A	125,000	0.67	0.83
B	623,000	1.00	1.00
C	171,000	1.18	1.24
total	919,000	--	--

Step 1 calculate total % change for each rating variable level

(1) level	(2) premium	(3) current	(4) indicated	(5) change	(6) off-bal	(7) overall	(8) total chg	(9) new prem
A	125,000	0.67	0.83	23.88%	0.9597	5%	24.84%	156,048
B	623,000	1.00	1.00	0.00%	0.9597	5%	0.77%	627,817
C	171,000	1.18	1.24	5.08%	0.9597	5%	5.90%	181,084
total	919,000	--	--	4.19%	0.9597	5%	5.00%	964,950

= Δs%

$$(5) = (4) / (3) - 1.0$$

$$(Tot5) = (5) \text{ weighted by } (2)$$

$$(6) = 1.0 / (1.0 + (Tot5)) = \text{off-balance} = 1 / (1 + \Delta s\%)$$

$$(7) = \text{given}$$

$$(8) = [1.0 + (5)] \times (6) \times [1.0 + (7)] - 1.0$$

$$(9) = (2) \times (1.0 + (8))$$

Step 2a cap relativity for non-base level A so that total change doesn't exceed

15% by solving for R below:

$$\begin{array}{lclclcl} R / \text{current} & \times & \text{off-bal} & \times & (1 + \text{overall}) & = & 1 + \text{max} \\ R / 0.67 & \times & 0.9597 & \times & 1.05 & = & 1.15 \end{array}$$

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$$R = 0.7646$$

new indicated relativity for level A

Step 2b calculate the premium shortfall created by the cap in step 2a

$$\begin{array}{lclclcl} \text{revised premium for A} & = & (9) & \times & R & / & (4) \\ & = & 156,048 & \times & 0.7646 & / & 0.8300 \\ & = & 143,750 & & & & \end{array}$$

$$\text{shortfall} = 156,048 - 143,750 = 12,298 \quad \text{<==== premium shortfall}$$

Step 3a redistribute this shortfall across levels B and C by increasing the base rate by a proportional amount

$$\text{premium for levels B \& C} = 627,817 + 181,084 = 808,902$$

$$\text{required base rate increase} = 12,298 / 808,902 = 1.520\% \quad \text{<==== base rate increase}$$

Step 3b BUT, we must now back out this base rate increase from level A otherwise the cap will be exceeded by that same amount

$$\begin{array}{lclclcl} \text{final indicated relativity for level A} & = & R & / & (1 + \text{base rate increase}) \\ & = & 0.7646 & / & 1.01520 \\ & = & 0.7531 & & \text{<==== final answer for proposed Level A relativity} \end{array}$$

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Problem Type: Limiting Premium Effect of a Single Variable (Non-Base Level)

W-14 (080) - (Problem 2)

Find Calculate the relativities that satisfy the given requirements.

overall rate change	12%
maximm premium increase for any level of the rating variable	20%

Given **Rating variable information prior to capping**

level	premium	current	indicated
A	132,000	0.68	0.85
B	724,000	1.00	1.00
C	155,000	1.18	1.24
total	1,011,000	--	--

Step 1 calculate total % change for each rating variable level

(1) level	(2) premium	(3) current	(4) indicated	(5) change	(6) off-bal	(7) overall	(8) total chg	(9) new prem
A	132,000	0.68	0.85	25.00%	0.9611	12%	34.56%	177,618
B	724,000	1.00	1.00	0.00%	0.9611	12%	7.65%	779,365
C	155,000	1.18	1.24	5.08%	0.9611	12%	13.12%	175,337
total	1,011,000	--	--	4.04%	0.9611	12%	12.00%	1,132,320

= Δs%

$$(5) = (4) / (3) - 1.0$$

$$(Tot5) = (5) \text{ weighted by } (2)$$

$$(6) = 1.0 / (1.0 + (Tot5)) = \text{off-balance} = 1 / (1 + \Delta s\%)$$

$$(7) = \text{given}$$

$$(8) = [1.0 + (5)] \times (6) \times [1.0 + (7)] - 1.0$$

$$(9) = (2) \times (1.0 + (8))$$

Step 2a cap relativity for non-base level A so that total change doesn't exceed

20% by solving for R below:

$$\begin{array}{lclclcl} R / \text{current} & \times & \text{off-bal} & \times & (1 + \text{overall}) & = & 1 + \text{max} \\ R / 0.68 & \times & 0.9611 & \times & 1.12 & = & 1.20 \end{array}$$

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$$R = 0.7580$$

new indicated relativity for level A

Step 2b calculate the premium shortfall created by the cap in step 2a

$$\begin{array}{lclclcl} \text{revised premium for A} & = & (9) & \times & R & / & (4) \\ & = & 177,618 & \times & 0.7580 & / & 0.8500 \\ & = & 158,400 & & & & \end{array}$$

$$\text{shortfall} = 177,618 - 158,400 = 19,218 \quad \text{<==== premium shortfall}$$

Step 3a redistribute this shortfall across levels B and C by increasing the base rate by a proportional amount

$$\text{premium for levels B \& C} = 779,365 + 175,337 = 954,702$$

$$\text{required base rate increase} = 19,218 / 954,702 = 2.013\% \quad \text{<==== base rate increase}$$

Step 3b BUT, we must now back out this base rate increase from level A otherwise the cap will be exceeded by that same amount

$$\begin{array}{lclclcl} \text{final indicated relativity for level A} & = & R & / & (1 + \text{base rate increase}) \\ & = & 0.7580 & / & 1.02013 \\ & = & 0.7431 & & \text{<==== final answer for proposed Level A relativity} \end{array}$$